

Systems of Equations – Quick Reference

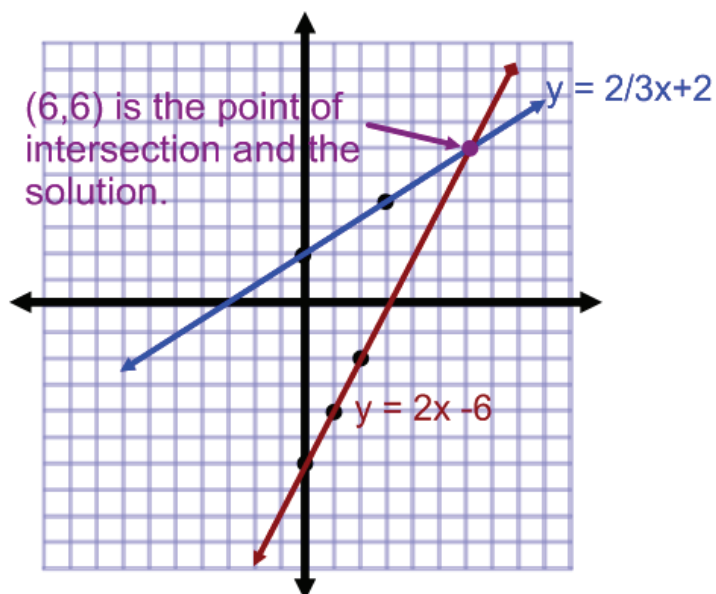
Two linear equations form a system of equations. You can solve a system of equations using one of three methods:

1. Graphing
2. Substitution Method
3. Linear Combinations Method

Graphing Systems of Equations

$$y = 2/3x + 2$$

$$y = 2x - 6$$



The solution to this system of equations is (6,6)

The solution to a system of equations is the **point of intersection**.

The **ordered pair** that is the point of intersection represents the solution that satisfies **BOTH** equations.

If two lines are **parallel** to each other, then there is **no solution**. The lines will never intersect.

If two lines lay **one on top of another** then there are **infinite solutions**. Every point on the line is a solution.

Substitution Method

Solve the following system of equations:

$$x - 2y = -10$$

$$y = 3x$$

$$x - 2y = -10$$

$$x - 2(3x) = -10$$

$$x - 6x = -10$$

$$-5x = -10$$

$$\frac{-5x}{-5} = \frac{-10}{-5}$$

$$x = 2$$

$$y = 3x$$

$$y = 3(2)$$

$$y = 6$$

Solution: (2, 6)

Since we know $y = 3x$, substitute $3x$ for y into the first equation.

Simplify: Multiply $2(3x) = 6x$.

Simplify: $x - 6x = -5x$

Solve for x by dividing both sides by -5 .

The x coordinate is 2.

Since we know that $x = 2$, we can substitute 2 for x into $y = 3x$.

The solution!

Linear Combinations (Addition Method)

Solve the following system of equations:

$$3x + 2y = 10$$

$$2x + 5y = 3$$

$$-2(3x + 2y = 10)$$

$$3(2x + 5y = 3)$$

$$-6x - 4y = -20$$

$$\frac{6x + 15y = 9}{11y = -11}$$

$$\frac{11y}{11} = \frac{-11}{11}$$

$$y = -1$$

$$2x + 5y = 3$$

$$2x + 5(-1) = 3$$

$$2x - 5 = 3$$

$$2x - 5 + 5 = 3 + 5$$

$$\frac{2x}{2} = \frac{8}{2}$$

$$x = 4$$

Create opposite terms. I'm creating opposite x terms.

Multiply to create opposite terms. Then add the like terms.

Solve for y by dividing both sides by 11.

The y coordinate is -1

Substitute -1 for y into one of the equations.

Solve for x !

The solution (4, -1)